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Description Implementation of the FVIBES, the Fuzzy Variable-Importance Based Eigenspace Separation algorithm as described in the paper by Ghashti, J.S., Hare, W., and J.R.J. Thompson (2025). Variable-Weighted Adjacency Constructions for Fuzzy Spectral Clustering. Submitted.

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clustering.accuracy *Clustering Accuracy with Optimal Label Matching*

Description

Computes the fraction of correctly classified observations between two label vectors after optimally matching cluster labels using `Thresher::matchLabels`.

Usage

```
clustering.accuracy(A, B)
```

Arguments

A An integer or character vector of cluster labels of length n .
 B An integer or character vector of cluster labels of length n .

Details

The function creates the contingency table `table(A, B)`, permutes columns to best align labels using `matchLabels`, and returns the sum of the diagonal divided by n .

Inputs must have equal length and the same number of unique labels; otherwise an error is given.

Value

A single numeric value in $[0, 1]$: the accuracy after optimal label matching.

References

K. R. Coombes (2025). *Thresher: Threshing and Reaping for Principal Components*. R package version 1.1.5.

See Also

[fuzzy.spectral.clustering](#), [gen.fuzzy](#), [plot.fuzzy](#), [matchLabels](#)

Examples

```
set.seed(1)
n <- 200
k <- 3
A <- sample.int(k, n, replace = TRUE) # assumed true clustering labels
perm <- sample.int(k) # assumed predicted labels (sampled by permutating)
B <- perm[A]
flips <- sample.int(n, 20) # add some error a few errors
B[flips] <- sample.int(k, length(flips), replace = TRUE)

clustering.accuracy(A, B)
```

compute.sigma	<i>Compute Locally-Adaptive Scaling Parameters from a Distance Matrix</i>
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Description

Derives pointwise scale parameters σ_i from a distance matrix, based on the r -th nearest neighbour distances. This is useful for constructing the adaptive similarity graphs proposed by Zelnik-Manor and Perona (2004).

Usage

```
compute.sigma(distance, r = NULL)
```

Arguments

distance	An $n \times n$ numeric (symmetric) distance matrix. Required.
r	Integer valued neighbourhood radius. If NULL, this value is estimated adaptively with find.radius .

Details

For each observation i , the function sorts the distances `distance[i,]`, excludes the zero self-distance, and takes the $(r + 1)$ smallest value, where σ_i reflects the distance to the r -th nearest neighbour for observation i .

Value

A list with components:

sigma	A numeric vector of length n , containing local scale parameters.
radius	The neighborhood radius r used.

References

Ghashti, J. S., Hare, W., and J. R. J. Thompson (2025). Variable-weighted adjacency constructions for fuzzy spectral clustering. Submitted.

Zelnik-Manor, L. and P. Perona (2004). Self-tuning spectral clustering. *Advances in Neural Information Processing Systems*, 17.

See Also

[make.adjacency](#), [gen.fuzzy](#), [plot.fuzzy](#), [rNN.dist](#), [find.radius](#), [compute.SNN](#), [fuzzy.spectral.clustering](#)

Examples

```
set.seed(1)
X <- matrix(rnorm(50), nrow = 10)
D <- as.matrix(dist(X))

res <- compute.sigma(D) # automatically determine r
res$sigma
res$radius

res2 <- compute.sigma(D, r = 3) # user-specified r
res2$sigma
```

compute.SNN

Shared-Nearest-Neighbours (SNN) Similarity from a Similarity Matrix

Description

Builds a Shared-Nearest-Neighbours (SNN) similarity matrix from an input similarity matrix `similarity`. For each pair of observations, the SNN score is the fraction of shared indices among their top- r neighbour lists.

Usage

```
compute.SNN(similarity, r)
```

Arguments

<code>similarity</code>	An $n \times n$ numeric <i>similarity</i> matrix. The diagonal is assumed to correspond to self-similarity and is ignored when forming neighbour lists.
<code>r</code>	Integer value number of nearest neighbours per observation used to compute SNN overlap.

Details

For each observation i , the function forms its neighbour set by ordering `similarity[i,]` in decreasing order, dropping i itself, and retaining the first r indices. For a pair (i, j) , the SNN similarity is

$$\text{SNN}(i, j) = \frac{|N_r(i) \cap N_r(j)|}{r},$$

i.e., the size of the intersection of their neighbour sets divided by r . The result is symmetric with ones on the diagonal.

Value

An $n \times n$ symmetric numeric matrix `SNN.S` with entries in $[0, 1]$.

References

Ghashti, J. S., Hare, W., and J. R. J. Thompson (2025). Variable-weighted adjacency constructions for fuzzy spectral clustering. Submitted.

Jarvis, R. A., and A. E. Patrick (1973). Clustering using a similarity measure based on shared near neighbors. *IEEE Transactions on Computers*, 22(11), 1025-1034.

See Also

[make.adjacency](#), [gen.fuzzy](#), [plot.fuzzy](#), [rNN.dist](#), [find.radius](#), [compute.sigma](#), [compute.SNN](#), [fuzzy.spectral.clustering](#)

Examples

```
set.seed(1)
X <- matrix(rnorm(50), nrow = 10)
D <- as.matrix(dist(X))
r <- 3
S <- exp(-D^2)
SNN <- compute.SNN(S, r)
head(SNN, 5)

# inspect average SNN similarity to nearest neighbour
rowMeans(SNN - diag(diag(SNN)))
```

Description

Computes fuzzy generalizations of the Adjusted Rand Index based on Frobenius inner products of membership matrices. These measures extends the Adjusted Rand Index to compare fuzzy partitions.

Usage

```
fari(a, b)
```

Arguments

a An $n \times G_1$ matrix of hard or fuzzy cluster memberships, where each row sums to 1.

b An $n \times G_2$ matrix of hard or fuzzy cluster memberships, where each row sums to 1.

Value

A single numeric value

fari The Frobenius Adjusted Rand index between a and b.

References

Andrews, J.L., Browne, R. and C.D. Hvingelby (2022). On Assessments of Agreement Between Fuzzy Partitions. *Journal of Classification*, 39, 326–342.

J.L. Andrews, FARI (2013). GitHub repository, <https://github.com/its-likeli-jeff/FARI>

Examples

```
set.seed(1)
a <- matrix(runif(600), nrow = 200, ncol = 3)
a <- a / rowSums(a)
b <- matrix(runif(600), nrow = 200, ncol = 3)
b <- b / rowSums(b)

fari(a, b)
```

find.radius

Adaptive Radius Selection by Natural Neighbours

Description

Implements a Natural Neighbour search to adaptively determine a neighbourhood radius r from a general distance matrix. The algorithm increases r until the number of points with zero in-degree in the r -nearest-neighbour graph no longer decreases, and returns this radius r .

Usage

```
find.radius(D)
```

Arguments

D An $n \times n$ numeric (symmetric) distance matrix.

Details

This procedure is adapted from the *Natural Neighbor (NaN)* algorithm by Zhu, Feng and Huang (2016). The algorithm works as follows:

1. For each integer r , build the directed r -nearest-neighbour graph from D .
2. Compute the in-degree counts, i.e., how many times each observation appears among others' first r neighbours.
3. Track the number of zero in-degree points; if this number stops decreasing when r increases, the algorithm stops and returns the current r , interpreted as the natural neighbour radius.

This provides a parameter-free way to adaptively set the neighbourhood size.

Value

A single integer r , the selected neighbourhood radius.

References

Zhu, Q., Feng, J., and J. Huang (2016). Natural neighbor: A self-adaptive neighborhood method without parameter K . *Pattern recognition letters*, 80, 30-36.

See Also

[make.adjacency](#), [gen.fuzzy](#), [plot.fuzzy](#), [rNN.dist](#), [compute.sigma](#), [compute.SNN](#), [fuzzy.spectral.clustering](#)

Examples

```
set.seed(1)
X <- matrix(rnorm(100), nrow = 20)
D <- as.matrix(dist(X))
r <- find.radius(D) # Estimate the natural neighbour radius
r
rNN.dist(D, r) # use selected r for rNN.dist
```

fuzzy.spectral.clustering

Fuzzy Spectral Clustering with Normalized Eigenvectors

Description

Implementation of the FVIBES algorithm by Ghashti, Hare, and Thompson (2025). Performs spectral clustering on a similarity (adjacency) matrix and returns either fuzzy c -means memberships or Gaussian mixture posterior probabilities computed on the leading normalized eigenvectors.

Usage

```
fuzzy.spectral.clustering(W = NULL,
                          k = NULL,
                          m = NULL,
                          method = "CM",
                          nstart = 10,
                          max.iter = 1000)
```

Arguments

W	A nonnegative $n \times n$ similarity (adjacency) matrix. Diagonal entries are set to 0 internally. Required.
k	Integer number of clusters. Required.
m	Fuzzy parameter for c-means, only used when method = "CM". When not provided, algorithm will set $m = 2$.
method	Clustering method applied to the spectral embedding with "CM" for fuzzy c-means with fclust , or "GMM" for Gaussian mixtures with mclust . Default is "CM".
nstart	Number of random starts for fclust::FKM when method = "CM".
max.iter	Maximum number of iterations for fclust::FKM when method = "CM".

Details

Let D be the diagonal degree matrix with $D_{ii} = \sum_j W_{ij}$. The routine forms the symmetrically normalized similarity $L = D^{-1/2}WD^{-1/2}$, (Ng, Jordan, and Weiss, 2001) computes its top k eigenvectors, stacks them in $X \in \mathbb{R}^{n \times k}$, and row-normalizes to Y with $Y_{i\cdot} = X_{i\cdot} / \|X_{i\cdot}\|_2$. Clustering is then performed in the rows of Y .

When method = "CM", clustering uses c-means (Bezdek, 1981) with **fclust::FKM** on Y with fuzzy parameter m , number of starts `nstart`, and maximum iterations `max.iter`. When method = "GMM", clustering uses Gaussian mixture models (see McLachlan and Krishnan, 2008) with **mclust::Mclust** with $G = k$ on Y .

Value

A list with components:

cluster	An integer vector of length n hard cluster labels.
u	An $n \times k$ matrix of fuzzy cluster memberships: for "CM", fuzzy c-means memberships U ; for "GMM", posterior probabilities Z .
evecs	The $n \times k$ matrix Y of row-normalized leading eigenvectors, i.e., the spectral embedding.
centers	Cluster centers for the embedding matrix Y .

References

- J.C. Bezdek (1981). *Pattern Recognition with Fuzzy Objective Function Algorithms*. Plenum Press, New York.
- Ferraro, M.B., Giordani, P., and A. Serafini (2019). fclust: An R Package for Fuzzy Clustering. *The R Journal*, 11.
- Ghashti, J. S., Hare, W., and J. R. J. Thompson (2025). Variable-weighted adjacency constructions for fuzzy spectral clustering. Submitted.
- McLachlan, G. and T. Krishnan (2008). *The EM algorithm and extensions*, Second Edition. John Wiley & Sons.
- Ng, A., Jordan, M., and Y. Weiss (2001). On spectral clustering: Analysis and an algorithm. *Advances in Neural Information Processing Systems*, 14.
- Scrucca, L., Fraley, C., Murphy, T.B., and A. E. Raftery (2023). *Model-Based Clustering, Classification, and Density Estimation Using mclust in R*. Chapman & Hall.

See Also

[make.adjacency](#), [gen.fuzzy](#), [plot.fuzzy](#), [rNN.dist](#), [find.radius](#), [compute.sigma](#), [compute.SNN](#), [npudensbw](#), [FKM](#), [Mclust](#)

Examples

```
set.seed(1)
d <- gen.fuzzy(n = 300,
              dataset = "spirals",
              noise = 0.18)

plot.fuzzy(d) # visualize data generating process

adj <- make.adjacency(data = d$X,
                    method = "vw",
                    isLocWeighted = TRUE,
                    isModWeighted = FALSE,
                    isSparse = FALSE,
                    ModMethod = NULL,
                    scale = FALSE,
                    sig = 1,
                    radius = NULL,
                    cv.method = "cv.ls") # vwla-id from paper

spectRes <- fuzzy.spectral.clustering(W = adj,
                                    k = 3,
                                    m = 1.5,
                                    method = "CM",
                                    nstart = 50,
                                    max.iter = 1000)

head(spectRes$u) # first 6 rows of U
```

```

plotDf <- list(
  X = d$X,
  y = factor(spectRes$cluster),
  U = spectRes$u,
  k = 3
)

plot.fuzzy(plotDf) # visualize results

clustering.accuracy(d$y, spectRes$cluster) # compare results

```

gen.fuzzy

Generate 2D synthetic datasets with known fuzzy memberships

Description

Simulates several 2D datasets together with fuzzy cluster memberships U . The memberships are defined by analytic density/curve proximity rules (detailed below) so they can be used as "ground truth" for fuzzy clustering and visualization (see [plot.fuzzy](#)).

Usage

```

gen.fuzzy(n = 500,
  dataset = c("gaussian", "hyperbolas", "spirals",
             "wedges", "rings", "worms", "random"),
  k = NULL,
  noise = 0.1,
  covType = c("spherical", "diagonal", "rotated", "correlated"),
  seed = NULL)

```

Arguments

n	Total number of observations.
dataset	Which data generator to use, with options "gaussian", "hyperbolas", "spirals", "wedges", "rings", "worms", or "random".
k	Number of clusters for dataset="random", ignored otherwise; if NULL, defaults to k = 20.
noise	Additive noise or curve-thickness parameter for applicable generators (see Details).
covType	Covariance structure for dataset="random"; one of "spherical", "diagonal", "rotated", "correlated".
seed	Optional seed for reproducibility.

Details

Let $X \in \mathbb{R}^{n \times 2}$ be the simulated observations and $U \in \mathbb{R}^{n \times k}$ the fuzzy memberships. For each dataset, memberships are defined below and row-normalized to sum to 1.

gaussian (k = 3). Three Gaussian components with means $(-2, 0)$, $(2, 0)$, $(0, 3)$ and covariances $([1, 0.3]; [0.3, 1])$, $([1, -0.3]; [-0.3, 1])$ and $([0.8, 0]; [0, 0.8])$. If component sizes are π_j , then $U_{ij} \propto \pi_j \phi_2(x_i | \mu_j, \Sigma_j)$.

hyperbolas (k = 5). One Gaussian near $(0, 0)$ and four hyperbola branches $\{(x, y) : (x \pm a)^2/b^2 - (y)^2/a^2 = 1\}$ and its rotated or flipped analogues, sampled along $t \in [-2, 2]$ with noise. For observation x_i , $w_{\text{ball}} = 50 \cdot \phi_2(x_i | (0, 0), 0.2I_2)$, and $w_{\text{hyp}, \ell} = \exp(-d^2(x_i, \mathcal{C}_\ell)/(\sigma^2))$, where $d(\cdot, \mathcal{C}_\ell)$ is minimum distance to branch ℓ for curve \mathcal{C} . We set $U_i \propto w$.

spirals (k = 3). Three spirals generated by $(r, \theta) \mapsto (x, y) = ((0.5 + 0.8t) \cos(\theta_s + t), (0.5 + 0.8t) \sin(\theta_s + t))$ with shifts $\theta_s \in \{0, 2\pi/3, 4\pi/3\}$, with additive noise. For each spiral s , $d_s = \min_{t \in [0, \pi]} \|x_i - \gamma_s(t)\|$, where $\gamma_s(t)$ is the parameterized spiral curve described above, and $U_{is} \propto \exp(-d_s^2/\sigma^2)$. Note, if $\|x_i\| < 1$, set $U_i \leftarrow (1 - \alpha)U_i + \alpha(1, 1, 1)/3$ with $\alpha = 0.5e^{-\|x_i\|}$ and normalize after.

wedges (k = 8). Eight angular wedges with inner/outer radii 1 and 4, respectively, with small gaps between wedges. For observation x_i with radius r and angle θ , membership to wedge j is $U_{ij} \propto \exp(-\delta(\theta, \theta_j)^2/\sigma^2)$, where δ is a wrapped angular distance to the wedge centre angle θ_j .

rings (k = 3). For $x_i \in \mathbb{R}^2$ and $r_i = \|x_i\|_2$, there are three concentric rings with radii $R_j \in \{1, 2.5, 4\}$ with widths $W_j \in \{0.3, 0.4, 0.5\}$ for $j = 1, 2, 3$. Let $w_{ij} = \exp(-(r_i - R_j)^2/W_j^2)$, then $U_{ij} = w_{ij} / \sum_{\ell=1}^3 w_{i\ell}$.

worms (k = 4). Each worm j is a sinusoidal curve parameterized on $t \in [0, 2\pi]$ by $\gamma_j(t) = (x(t), y_j(t))$ with $x(t) = 2(t - \pi)$, $y_j(t) = A_j \sin(f_j t + \phi_j) + y_j^{\text{off}}$, with amplitudes A_j , frequencies f_j , phases ϕ_j , and vertical offsets y_j^{off} . For observation $x_i \in \mathbb{R}^2$, the distance to worm j is $d_j(x_i) = \min_{t \in [0, 2\pi]} \|x_i - \gamma_j(t)\|_2$. Then $w_{ij} = \exp(-d_j(x_i)^2/\sigma^2)$, and $U_{ij} = w_{ij} / \sum_{\ell=1}^4 w_{i\ell}$.

random (k is user-specified). Mixture of k Gaussians with common covariance determined by `covType` with random centres in $[0, 30]^2$ and random cluster sizes. With mixture weights π_j , $U_{ij} \propto \pi_j \phi_2(x_i | \mu_j, \Sigma)$.

Value

A list with components:

X	An $n \times 2$ numeric matrix of observations.
U	An $n \times k$ matrix of probabilistic/fuzzy cluster memberships.
y	A vector length n of integers corresponding to hard cluster labels.
k	Number of clusters.
centres, clusSz, covMatrix	Returned only for <code>dataset="random"</code> : the centres, cluster sizes, and common covariance used.

Notes

The noise argument is used by "gaussian", "hyperbolas", "spirals", "rings", and "worms"; it is ignored by "wedges".

See Also[plot.fuzzy](#)**Examples**

```

set.seed(1)

g <- gen.fuzzy(n = 600, dataset = "gaussian", seed = 1)
plot.fuzzy(g, plotFuzzy = TRUE, colorCluster = TRUE)

s <- gen.fuzzy(n = 450, dataset = "spirals", noise = 0.2, seed = 1)
plot.fuzzy(s, plotFuzzy = TRUE, colorCluster = FALSE)

r <- gen.fuzzy(n = 800, dataset = "random", k = 15, covType = "rotated", seed = 1)
plot.fuzzy(r, plotFuzzy = TRUE, colorCluster = TRUE)

```

make.adjacency

*A General Framework for Adjacency Matrix Construction***Description**

Builds an $n \times n$ adjacency matrix from data using Euclidean or variable-weighted distances, with optional locally-adaptive scalings and optional variable weighting by shared-nearest-neighbours (SNN), similarity ranks (SIM), or both. The options reproduce a family of adjacency matrices including the variants described by Ghashti, Hare and Thompson (2025).

Usage

```

make.adjacency(data,
               method = "vw",
               isLocWeighted = FALSE,
               isModWeighted = FALSE,
               isSparse = FALSE,
               ModMethod = NULL,
               scale = FALSE,
               sig = 1,
               radius = NULL,
               cv.method = "cv.ls")

```

Arguments

data	Numeric matrix or data frame of size $n \times p$. Required.
method	Distance construction "eu" for Euclidean; "vw" for variable-weighted scaling (see Details). Defaults to "v".
isLocWeighted	Logical. If TRUE, use locally-adaptive scalings σ_i (Zelnik–Perona) to self-tune the kernel; otherwise use a global scale sig. Defaults to FALSE.

isModWeighted	Logical. If TRUE, apply a weighting matrix M based on SNN and/or SIM (see Details). Defaults to FALSE
isSparse	Logical. If TRUE and isModWeighted = TRUE, then SNN (ModMethod = "snn") and/or SIM (ModMethod = "sim") arguments creates a sparse adjacency matrix (see Details). Defaults to FALSE.
ModMethod	One of "snn", "sim", or "both" when isModWeighted=TRUE.
scale	Logical; standardize columns of data before distance construction.
sig	Positive numeric value for global kernel width, used only when isLocWeighted=FALSE.
radius	Integer r . If NULL, r is estimated with <code>find.radius</code> on the constructed distance matrix.
cv.method	Bandwidth selector for method="vw" passed to <code>np: :npudensbw</code> ; one of "cv.ml" or "cv.ls".

Details

Step 1: Distance.

- method="eu": $D_{ij} = \|x_i - x_j\|_2$.
- method="vw": compute product-kernel bandwidths h via `np: :npudensbw`, set feature-weights $w_j = 1/h_j^2$, rescale data as $\tilde{x}_{ij} = \sqrt{w_j} x_{ij}$, then $D_{ij} = \|\tilde{x}_i - \tilde{x}_j\|_2$. (Variable-weighted metric.)

Step 2: Similarity kernel.

- *Locally-adaptive scaling* from Zelnik-Manor: if isLocWeighted=TRUE, compute σ_i as the distance to the r -th neighbour with `compute.sigma` and set

$$S_{ij} = \exp\left(-D_{ij}^2/(\sigma_i\sigma_j)\right), \quad S_{ii} = 1.$$

- *Global scale*: if isLocWeighted=FALSE,

$$S_{ij} = \exp\left(-D_{ij}^2/\sigma^2\right), \quad S_{ii} = 1.$$

Step 3: Weighting Matrix (optional).

Let SNN_{ij} be the shared- r -NN overlap fraction (see `compute.SNN`) for observations i and j , and ρ_i be the $(r+1)$ -largest entry of observation i in matrix S . Define $\text{SIM}_{ij} = \sqrt{\rho_i\rho_j}$. For isModWeighted=TRUE we have the following options

- ModMethod="snn": $M_{ij} = \begin{cases} 0.5(1 + \text{SNN}_{ij}), & \text{if isSparse=FALSE,} \\ \text{SNN}_{ij}, & \text{if isSparse=TRUE.} \end{cases}$
- ModMethod="sim": $M_{ij} = \begin{cases} 0.5(1 + \text{SIM}_{ij}), & \text{if isSparse=FALSE,} \\ \text{SIM}_{ij}, & \text{if isSparse=TRUE.} \end{cases}$
- ModMethod="both": $M_{ij} = \begin{cases} 0.25(1 + \text{SIM}_{ij})(1 + \text{SNN}_{ij}), & \text{if isSparse=FALSE,} \\ \text{SIM}_{ij} \cdot \text{SNN}_{ij}, & \text{if isSparse=TRUE.} \end{cases}$

The returned adjacency is $W = S \circ M$ when isModWeighted = TRUE, otherwise $W = S$. These choices align with the table of named adjacency matrices (see Mapping below).

Value

An $n \times n$ numeric adjacency matrix W with ones on the diagonal.

Mapping to named adjacency matrices

Relating to the paper by Ghashti, Hare, and Thompson (2025), let "vw" denote the variable-weighted distance method="vw" and "eu" for the traditional squared Euclidean distance; "la" denotes locally-adaptive scaling when isLocWeighted=TRUE (Zelnik-Manor and Perona, 2004); "id" denotes identity for isModWeighted = FALSE, and "sim", "snn" and "simsnn" denote weightings for M described above.

To reproduce results from the 2025 paper, below are a few examples of adjacency construction:

- vw-id: $\exp(-D^2/\sigma^2)$ with method="vw", isLocWeighted=FALSE, isModWeighted=FALSE.
- vwla-id: $\exp(-D^2/(\sigma_i\sigma_j))$ with method="vw", isLocWeighted=TRUE, isModWeighted=FALSE.
- vw-sim: $0.5 \exp(-D^2/\sigma^2) (1+\text{SIM})$ with method="vw", isLocWeighted=FALSE, isModWeighted=TRUE, ModMethod="sim", isSparse=FALSE.
- vw-snns: $0.5 \exp(-D^2/\sigma^2) (1+\text{SNN})$ with method="vw", isLocWeighted=FALSE, isModWeighted=TRUE, ModMethod="snn", isSparse=TRUE.
- vw-simsnns: $0.25 \exp(-D^2/\sigma^2) (1+\text{SIM})(1+\text{SNN})$ with method="vw", isLocWeighted=FALSE, isModWeighted=TRUE, ModMethod="both", isSparse=TRUE.

Also note that:

- If radius is NULL, r is chosen adaptively via `find.radius` on the constructed distance matrix.
- method="vw" requires `npudensbw` for variable weighted bandwidths, with default `np: npudensbw(data, bwmethod = cv.method, nmulti = 3)` (Hayfield and Racine, 2008).

Notes

- When r is determined by `find.radius`, we implement a modified version of the Natural Neighbors algorithm from Zhu et al. (2016).
- SNN is a modified version of the Shared Nearest Neighbors algorithm from Jarvis and Patrick (1973).
- More information on locally-adaptive scalings are seen in Zelnik-Manor and Perona (2004).

References

- Ghashti, J. S., Hare, W., and J. R. J. Thompson (2025). Variable-weighted adjacency constructions for fuzzy spectral clustering. Submitted.
- Hayfield, T., and J. S. Racine (2008). Nonparametric Econometrics: The np Package. *Journal of Statistical Software* 27(5).
- Jarvis, R. A., and A. E. Patrick (1973). Clustering using a similarity measure based on shared near neighbors. *IEEE Transactions on Computers*, 22(11), 1025-1034.
- Zelnik-Manor, L., and P. Perona (2004). Self-tuning spectral clustering. *Advances in Neural Information Processing Systems*, 17.
- Zhu, Q., Feng, J., and J. Huang (2016). Natural neighbor: A self-adaptive neighborhood method without parameter K . *Pattern Recognition Letters*, 80, 30-36.

See Also

[gen.fuzzy](#), [plot.fuzzy](#), [rNN.dist](#), [find.radius](#), [compute.sigma](#), [compute.SNN](#), [fuzzy.spectral.clustering](#), [npudensbw](#)

Examples

```
set.seed(1)
X <- scale(matrix(rnorm(200), 100, 2))

W1 <- make.adjacency(X,
  method = "eu",
  isLocWeighted = TRUE) # "eula-id" named adjacency

W2 <- make.adjacency(X,
  method = "vw",
  isLocWeighted = TRUE) # "vwla-id" named adjacency

# compare W(xi,xj) i,j = 1,...,5 for eu/vw pair W1 and W2
W1[1:5,1:5]
W2[1:5,1:5]

W3 <- make.adjacency(X,
  method = "eu",
  isLocWeighted = TRUE,
  isModWeighted = TRUE,
  ModMethod = "snn",
  isSparse = FALSE) # "eula-snn" named adjacency

W4 <- make.adjacency(X,
  method = "vw",
  isLocWeighted = TRUE,
  isModWeighted = TRUE,
  ModMethod = "snn",
  isSparse = FALSE) # "vwla-snn" named adjacency

# compare W(xi,xj) i,j = 1,...,5 for eu/vw pair W3 and W4
W3[1:5,1:5]
W4[1:5,1:5]
```

plot.fuzzy

Plot 2D Fuzzy Data with Optional Uncertainty Sizing and Cluster Colouring

Description

Creates a [ggplot](#) of 2D points with optional colouring by hard labels and optional observation-size mapping to fuzzy uncertainty.

Usage

```
## S3 method for class 'fuzzy'
plot(x, plotFuzzy = TRUE, colorCluster = TRUE, ...)
```

Arguments

x	A list as returned by gen.fuzzy , containing X, U, y, and k.
plotFuzzy	Logical; if TRUE, map observation size to uncertainty $1 - \max_j U_{ij}$.
colorCluster	Logical; if TRUE, colour points by the hard cluster label y.
...	Additional arguments (currently unused).

Details

The plotting aesthetics can be modified as follows:

- If plotFuzzy and colorCluster are both TRUE (default), the plot contains cluster coloured observations that are size scaled by uncertainty.
- If only plotFuzzy is TRUE, the plot contains monochrome coloured observations that are size scaled by uncertainty.
- If only colorCluster is TRUE, the plot contains cluster coloured observations with fixed size.
- If plotFuzzy and colorCluster are both FALSE, the plot is monochrome coloured observations with fixed size.

Value

A ggplot object.

References

H. Wickham (2016). *ggplot2: Elegant Graphics for Data Analysis*. Springer-Verlag New York.

See Also

[gen.fuzzy](#), [ggplot](#)

Examples

```
set.seed(1)
d1 <- gen.fuzzy(n = 600, dataset = "gaussian", seed = 1)
p1 <- plot.fuzzy(d1)
p1 # default

p2 <- plot.fuzzy(d1, plotFuzzy = TRUE, colorCluster = FALSE)
p2 # only uncertainty sizing, monochrome

p3 <- plot.fuzzy(d1, plotFuzzy = FALSE, colorCluster = TRUE)
p3 # only coloured by cluster, no uncertainty sizing
```

`rNN.dist`*Compute r-Nearest Neighbours from a Distance Matrix*

Description

Given a symmetric distance matrix, returns the indices of the r nearest neighbours for each observation.

Usage

```
rNN.dist(D, r)
```

Arguments

<code>D</code>	An $n \times n$ numeric (symmetric) distance matrix.
<code>r</code>	Integer indicating the number of nearest neighbours to extract for each observation.

Details

For each row i of `D`, the function orders the distances $D[i, \cdot]$, excludes the self-distance, and returns the indices of the first r smallest distances. This provides the indices of the r nearest neighbours of observation i .

Value

An $n \times r$ integer matrix, where row i contains the indices of the r nearest neighbours of observation i .

References

Ghashti, J. S., Hare, W., and J. R. J. Thompson (2025). Variable-weighted adjacency constructions for fuzzy spectral clustering. Submitted.

See Also

[make.adjacency](#), [gen.fuzzy](#), [plot.fuzzy](#), [find.radius](#), [compute.sigma](#), [compute.SNN](#), [fuzzy.spectral.clustering](#)

Examples

```
set.seed(1)
X <- matrix(rnorm(20), nrow = 5)
D <- as.matrix(dist(X))
rNN.dist(D, r = 2) # find 2 nearest neighbours for each row
```

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